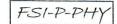
# I.F.S. EXAM-(M)2017



PHYSICS Paper – I

Time Allowed : Three Hours

Maximum Marks : 200

# **Question Paper Specific Instructions**

Please read each of the following instructions carefully before attempting questions :

There are **EIGHT** questions in all, out of which **FIVE** are to be attempted.

Questions no. 1 and 5 are **compulsory**. Out of the remaining **SIX** questions, **THREE** are to be attempted selecting at least **ONE** question from each of the two Sections A and B.

Attempts of questions shall be counted in sequential order. Unless struck off, attempt of a question shall be counted even if attempted partly. Any page or portion of the page left blank in the Question-cum-Answer Booklet must be clearly struck off.

All questions carry equal marks. The number of marks carried by a question/part is indicated against it.

Answers must be written in **ENGLISH** only.

Unless otherwise mentioned, symbols and notations have their usual standard meanings.

Assume suitable data, if necessary and indicate the same clearly.

Neat sketches may be drawn, wherever required.

## Useful Constants :

Electron charge $(e)$	$= 1.602 \times 10^{-19} \mathrm{C}$
Electron rest mass $(m_e)$	$= 9.109  imes 10^{-31} \text{ kg}$
Proton mass $(ni_p)$	$= 1.672 \times 10^{-27} \text{ kg}$
Vacuum permittivity ( $\varepsilon_0$ )	= $8.854 \times 10^{-12}$ farad/m
Vacuum permeability $(\mu_0)$	= $1.257 \times 10^{-6}$ henry/m
Velocity of light in free space $(c)$	$= 3 \times 10^8 \text{ m/s}$
Boltzmann constant (k)	= $1.380 \times 10^{-23}$ J/K
Electron volt (eV)	$= 1.602 \times 10^{-19} \mathrm{J}$
Planck constant $(h)$	$= 6.626 \times 10^{-34} \text{ Js}$
Stefan constant ( $\sigma$ )	= $5.67 \times 10^{-8} \mathrm{Wm^{-2}  K^{-4}}$
Avogadro number (N)	$= 6.022 \times 10^{26} \ \mathrm{kmol^{-1}}$
Gas constant $(R)$	= $8.31 \times 10^3 \text{ J kmol}^{-1} \text{ K}^{-1}$
$\exp\left(1 ight)$	= 2.718

## SECTION A

## Q1. Answer the following :

(a) A bead slides on a wire in the shape of a cycloid described by the equations

 $\mathbf{x} = \mathbf{a} \left( \theta - \sin \theta \right)$ 

 $y = a (1 + \cos \theta)$  with  $0 \le \theta \le 2\pi$ .

Find the Lagrangian and equation of motion.

- (b) Show that the relativistic invariance laws of conservation of momentum lead to the concepts of variation of mass with velocity and mass energy equivalence.
- (c) A parallel beam of light of wavelength 5890 Å is incident at an angle of 30° on a plane transmission grating with 15000 lines/inch. Find the highest order of spectrum that can be observed.
- (d) Discuss absorption loss in an optical fibre comparing and contrasting the intrinsic and extrinsic absorption mechanisms.
- (e) Although the principle of operation of a basic LASER is based upon two energy levels, why does one need a 3-level or a 4-level scheme to achieve satisfactory lasing ? Explain your answer with special reference to a Ruby-laser.
- Q2. (a) Discuss the mechanics of a system of point particles with special emphasis on the conservation theorems. How can we extend the results to a system with continuous mass distribution ?
  - (b) (i) State and prove Hamilton's principle and use it to prove that the shortest distance between two points in space is a straight line joining them.
    - (ii) Use Hamiltonian mechanics to find the differential equation for planetary motion, moving under force  $f(r) = -\frac{k}{r^2}$  and prove that the areal velocity is constant. 8+7=15
  - (c) (i) What is Holography?
    - (ii) Show with simple diagrams, how a hologram is written and read using a laser.
    - (iii) Mention some important applications of holography.

FSI-P-PHY

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3+8+4=15

- **Q3.** (a) State the fundamental postulates of Einstein's special theory of relativity. Deduce Lorentz transformation equation and discuss how this accounts for the phenomenon of length contraction.
  - (b) Discuss the properties of Cornu spiral. Show that the spiral can be used to obtain the intensity distribution in the Fresnel's diffraction pattern due to a straight edge.
  - (c) (i) Using the concept of spontaneous and stimulated emission of radiation, obtain the relation between Einstein's A and B coefficients.
    - (ii) What is the physical significance of Einstein's A coefficient ?
    - (iii) Justify why lasing action is much more difficult at X-ray frequency than in case of infrared frequency spectrum. 10+5+5=20

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- **Q4.** (a) (i) In a Michelson's interferometer, 100 fringes cross the field of view when the movable mirror is displaced through  $2.894 \times 10^{-3}$  cm. Calculate the wavelength of the monochromatic source of light.
  - (ii) A shift of 200 fringes is observed when the movable mirror of a Fabry-Pérot interferometer is shifted by 0.0298 mm. Calculate the wavelength of the incident radiation. 8+7=15
  - (b) State and explain Fermat's principle of extremum path and use the same to deduce the laws of reflection and refraction of light. 10
  - (c) (i) Explain the reason for pulse broadening due to intermodal and material dispersion. Deduce the relation of pulse broadening for intermodal dispersion in optical fiber.
    - (ii) A step index fiber in air has a numerical aperture of 0.16, a core refractive index of 1.45 and a core diameter of 60  $\mu$ m. Determine the normalized frequency for the fiber when light at a wavelength of 0.8  $\mu$ m is transmitted. Also estimate the number of guided modes propagating in the fiber. 10+5=15

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#### SECTION B

#### Q5. Answer the following :

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(a) In a one-dimensional device, the charge density is given by

$$\rho_{\rm V} = \rho_0 \frac{\rm x}{\rm a}$$

If E = 0 at x = 0 and V = 0 at x = a, find V and E using Laplace equation of electrostatics.

- (b) State and explain the Biot-Savart law. Derive an expression for the magnetic field at a point due to an infinitely long straight current carrying conductor.
- (c) Write down the four Maxwell's equations and explain the contribution of Maxwell in the development of these equations.
- (d) Prove the thermodynamic relation :

$$\left(\frac{\partial S}{\partial V}\right)_{T} = \left(\frac{\partial P}{\partial T}\right)_{V}$$

and hence show that

$$\frac{dP}{dt} = \frac{L}{T\left(V_2 - V_1\right)};$$

all the terms have their usual meanings.

- (e) Describe neutron star on the basis of Fermi-Dirac statistics and obtain the condition of critical mass for a neutron star.
- Q6. (a) Use the method of electric images to find the electric field on the surface of a grounded conducting sphere. 10
  - (b) (i) State Faraday's law of electromagnetic induction and prove that it can be expressed in the following vector form :

$$\operatorname{Curl} \overrightarrow{\mathbf{E}} = - \frac{\partial \overrightarrow{\mathbf{B}}}{\partial t}$$

with  $\overrightarrow{E}$  and  $\overrightarrow{B}$  being the electric and magnetic fields.

(ii) A coil of 10 turns has dimension 9 cm  $\times$  7 cm. It rotates at the rate of 15 $\pi$  rad/sec in a uniform field whose flux density is 0.6 weber/m<sup>2</sup>. What is the maximum e.m.f. induced in the coil? 10+5=15

 $8 \times 5 = 40$ 

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