WARNING : Any in th	malpra ne Exar	actice or any attempt to commi nination will DISQUALIFY THE	t any kind of malpractice CANDIDATE.
	PAPE	R-II MATHEMATICS-	2014
Version Code	B2	Question Booklet Serial Number :	7235967
Time : 150 Minutes		Number of Questions : 120	Maximum Marks : 480
Name of Candida	ate		
Roll Number			
Signature of Can	didate		
	INST	RUCTIONS TO THE CANDI	DATE

- 1. Please ensure that the VERSION CODE shown at the top of this Question Booklet is the same as that shown in the OMR Answer Sheet issued to you. If you have received a Question Booklet with a different VERSION CODE, please get it replaced with a Question Booklet with the same VERSION CODE as that of the OMR Answer Sheet from the invigilator. THIS IS VERY IMPORTANT.
- 2. Please fill in the items such as name, signature and roll number of the candidate in the columns given above. Please also write the Question Booklet Sl. No. given at the top of this page against item 5 in the OMR Answer Sheet.
- 3. Please read the instructions given in the OMR Answer Sheet for marking answers. Candidates are advised to strictly follow the instructions contained in the OMR Answer Sheet.
- 4. This Question Booklet contains 120 questions. For each question, five answers are suggested and given against (A), (B), (C), (D) and (E) of which, only one will be the Most Appropriate Answer. Mark the bubble containing the letter corresponding to the 'Most Appropriate Answer' in the OMR Answer Sheet, by using either Blue or Black ball-point pen only.
- 5. Negative Marking: In order to discourage wild guessing, the score will be subject to penalization formula based on the number of right answers actually marked and the number of wrong answers marked. Each correct answer will be awarded FOUR marks. One mark will be deducted for each incorrect answer. More than one answer marked against a question will be deemed as incorrect answer and will be negatively marked.

IMMEDIATELY AFTER OPENING THIS QUESTION BOOKLET, THE CANDIDATE SHOULD VERIFY WHETHER THE QUESTION BOOKLET ISSUED CONTAINS ALL THE 120 QUESTIONS IN SERIAL ORDER. IF NOT, REQUEST FOR REPLACEMENT.

DO NOT OPEN THE SEAL UNTIL THE INVIGILATOR ASKS YOU TO DO SO.

SEAL

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PLEASE ENSURE THAT THIS BOOKLET CONTAINS 120 QUESTIONS SERIALLY NUMBERED FROM 1 TO 120. (Printed Pages : 32)

1. The number of solutions for the system of equations 2x + y = 4, 3x + 2y = 2, and

x + y = -2 is

(A) 1	(B) 2	(C) 3
(D) infinitely many	(E) 0	

- 2. The number of solutions of the inequation |x-2| + |x+2| < 4 is
 - (A) 1 (B) 2 (C) 4 (D) 0 (E) infinite
- 3. The shaded region shown in the figure is given by the inequations



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4. Let p, q and r be any three logical statements. Which one of the following is true?

(A)
$$\sim [p \land (\sim q)] \equiv (\sim p) \land q$$

(B) $\sim (p \lor q) \land (\sim r) \equiv (\sim p) \lor (\sim q) \lor (\sim r)$
(C) $\sim [p \lor (\sim q)] \equiv (\sim p) \land q$
(D) $\sim [p \land (\sim q)] \equiv (\sim p) \land \sim q$
(E) $\sim [p \land (\sim q)] \equiv p \land q$

5. The truth values of p, q and r for which $(p \land q) \lor (\sim r)$ has truth value F are respectively (A) F, T, F (B) F, F, F (C) T, T, T (D) T, F, F (E) F, F, T

6. $\sim [(\sim p) \land q]$ is logically equivalent to

(A)
$$\sim (p \lor q)$$

(B) $\sim [p \land (\sim q)]$
(C) $p \land (\sim q)$
(D) $p \lor (\sim q)$
(E) $(\sim p) \lor (\sim q)$

7. Let
$$\theta \in \left[0, \frac{\pi}{2}\right]$$
. Which one of the following is true?
(A) $\sin^2 \theta > \cos^2 \theta$ (B) $\sin^2 \theta < \cos^2 \theta$ (C) $\sin \theta > \cos \theta$
(D) $\cos \theta > \sin \theta$ (E) $\sin \theta + \cos \theta \le \sqrt{2}$
8. The value of $\sin^{-1}\left(\frac{2\sqrt{2}}{3}\right) + \sin^{-1}\left(\frac{1}{3}\right)$ is equal to
(A) $\frac{\pi}{6}$ (B) $\frac{\pi}{4}$ (C) $\frac{\pi}{2}$ (D) $\frac{2\pi}{3}$ (E) 0

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9.	If $ab < 1$ and $\cos \theta$	$-1\left(\frac{1-a^2}{1+a^2}\right)+\cos^{-1}\left(\frac{1-a^2}{1+a^2}\right)$	$\left(\frac{1-b^2}{1+b^2}\right) = 2\tan^{-1}x$, then x is equal to)	. 3
	(A) $\frac{a}{1+ab}$	(B) $\frac{a}{1-ab}$	(C) $\frac{a-b}{1+ab}$	(D) $\frac{a+b}{1+ab}$	(E) $\frac{a+b}{1-ab}$	*
10.	The value of tan	(1°) + tan(89°) is e	qual to			
	(A) $\frac{1}{\sin 1^{\circ}}$	(B) $\frac{2}{\sin 2^{\circ}}$	(C) $\frac{2}{\sin 1^\circ}$	(D) $\frac{1}{\sin 2^{\circ}}$	(E) $\frac{\sin 2^\circ}{2}$	•
11.	Let $s_n = \cos\left(\frac{n\pi}{10}\right)$), $n = 1, 2, 3,$ The	en the value of $\frac{1}{s_1}$	$\frac{s_1 s_2 \dots s_{10}}{s_2 + \dots + s_{10}}$ is equ	ual to	
	(A) $\frac{1}{\sqrt{2}}$	(B) $\frac{\sqrt{3}}{2}$	(C) 2√2	(D) 0	(E) $\frac{1}{2}$	
12.	$\cos^{-1}\left(\cos\left(\frac{7\pi}{5}\right)\right)$)=			Juli Supera	
	(A) $\frac{3\pi}{5}$	(B) $\frac{2\pi}{5}$	(C) $\frac{-7\pi}{5}$	(D) $\frac{7\pi}{5}$	(E) $\frac{-2\pi}{5}$	•
13.	The value of sec ²	$(\tan^{-1} 3) + \operatorname{cosec}^2 ($	$\cot^{-1}2$ is equal to	5		
	(A) 5	(B) 13	(C) 15	(D) 23	(E) 25	3
14.	If $\sin\theta + \csc\theta$	= 2, then the value	of $\sin^6 \theta + \csc$	$^{6}\theta$ is equal to		
	(A) 0	(B) 1	(C) 2	(D) 2 ³	(E) 2 ⁶	

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[P.T.O.]

15.	If $0 < x < \pi$, then		$18\sin 4x + 12\sin 2x$	_	
		$\sin 7x + 6\sin x$	$5x+12\sin 3x$		
	(A) $2\sin x$	(B) $\sin x$	(C) $\sin 2x$	(D) $2\cos x$	(E) $\cos x$
16.			two opposite vertices $y = 2x + k$, then	ces of a rectangle the value of k is	. If the other two
	(A) 4	(B) 3	(C) -4	(D) -3	(E) 1
17.	The circumcentre	of the triangle wit	h vertices (8,6),(8	,-2) and (2,-2) is	at the point
	(A) (2, -1)	(B) (1,-2)	(C) (5,2)	(D) (2,5)	(E) (4, 5)
18.	The ratio by which $(-4, 7)$ and $(6, -3)$		-7 = 0 divides the	e straight line joini	ng the points
	(A) 1:4	(B) 1 : 2	(C) 1 : 1	(D) 2 : 3	(E) 1 : 3
19.	The number of point $x^2 - y^2 = 512$ is	pints (a,b) , where	a and b are posit	ive integers, lying	on the hyperbola
	(A) 3	(B) 4	(C) 5	(D) 6	(E) 7

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and the second

- 20. If p is the length of the perpendicular from the origin to the line whose intercepts with the coordinate axes are $\frac{1}{3}$ and $\frac{1}{4}$ then the value of p is
 - (A) $\frac{3}{4}$ (B) $\frac{1}{12}$ (C) 5 (D) 12 (E) $\frac{1}{5}$

21. The slope of the straight line joining the centre of the circle $x^2 + y^2 - 8x + 2y = 0$ and the vertex of the parabola $y = x^2 - 4x + 10$ is

- (A) $\frac{-5}{2}$ (B) $\frac{-7}{2}$ (C) $\frac{-3}{2}$ (D) $\frac{5}{2}$ (E) $\frac{7}{2}$
- 22. A straight line perpendicular to the line 2x+y=3 is passing through (1,1). Its y-intercept is
 - (A) 1 (B) 2 (C) 3 (D) $\frac{1}{2}$ (E) $\frac{1}{3}$
- 23. If p and q are respectively the perpendiculars from the origin upon the straight lines whose equations are $x \sec \theta + y \csc \theta = a$ and $x \cos \theta y \sin \theta = a \cos 2\theta$, then $4p^2 + q^2$ is equal to
 - (A) $5a^2$ (B) $4a^2$ (C) $3a^2$ (D) $2a^2$ (E) a^2

24. The shortest distance between the circles $(x-1)^2 + (y+2)^2 = 1$ and $(x+2)^2 + (y-2)^2 = 4$ is (A) 1 (B) 2 (C) 3 (D) 4 (E) 5

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- 25. The centre of the circle whose radius is .5 and which touches the circle $x^2 + y^2 2x 4y 20 = 0$ at (5, 5) is
 - (A) (10, 5) (B) (5, 8) (C) (5, 10) (D) (8, 9) (E) (9, 8)
- 26. A circle passes through the points (0,0) and (0,1) and also touches the circle $x^2 + y^2 = 16$. The radius of the circle is
 - (A) 1 (B) 2 (C) 3 (D) 4 (E) 5
- 27. A circle of radius $\sqrt{8}$ is passing through origin and the point (4, 0). If the centre lies on the line y = x, then the equation of the circle is
 - (A) $(x-2)^2 + (y-2)^2 = 8$ (B) $(x+2)^2 + (y+2)^2 = 8$ (C) $(x-3)^2 + (y-3)^2 = 8$ (D) $(x+3)^2 + (y+3)^2 = 8$ (E) $(x-4)^2 + (y-4)^2 = 8$
- 28. The parametric form of the ellipse $4(x+1)^2 + (y-1)^2 = 4$ is
 - (A) $x = \cos \theta 1$, $y = 2\sin \theta 1$ (B) $x = 2\cos \theta - 1$, $y = \sin \theta + 1$ (C) $x = \cos \theta - 1$, $y = 2\sin \theta + 1$ (D) $x = \cos \theta + 1$, $y = 2\sin \theta + 1$
 - (E) $x = \cos \theta + 1$, $y = 2\sin \theta 1$

29. A point P on an ellipse is at a distance 6 units from a focus. If the eccentricity of the ellipse is $\frac{3}{5}$, then the distance of P from the corresponding directrix is

- (A) $\frac{8}{5}$ (B) $\frac{5}{8}$ (C) 10 (D) 12 (E) 15
- 30. If the length of the latus rectum and the length of transverse axis of a hyperbola are $4\sqrt{3}$ and $2\sqrt{3}$ respectively, then the equation of the hyperbola is
 - (A) $\frac{x^2}{3} \frac{y^2}{4} = 1$ (B) $\frac{x^2}{3} \frac{y^2}{9} = 1$ (C) $\frac{x^2}{6} \frac{y^2}{9} = 1$ (D) $\frac{x^2}{6} - \frac{y^2}{3} = 1$ (E) $\frac{x^2}{3} - \frac{y^2}{6} = 1$
- 31. If the eccentricity of the hyperbola $\frac{x^2}{a^2} \frac{y^2}{b^2} = 1$ is $\frac{5}{4}$ and 2x + 3y 6 = 0 is a focal chord of the hyperbola, then the length of transverse axis is equal to
 - (A) $\frac{12}{5}$ (B) 6 (C) $\frac{24}{7}$ (D) $\frac{24}{5}$ (E) $\frac{12}{7}$
- 32. The length of the transverse axis of a hyperbola is $2\cos\alpha$. The foci of the hyperbola are the same as that of the ellipse $9x^2 + 16y^2 = 144$. The equation of the hyperbola is

(A)
$$\frac{x^2}{\cos^2 \alpha} - \frac{y^2}{7 - \cos^2 \alpha} = 1$$
 (B) $\frac{x^2}{\cos^2 \alpha} - \frac{y^2}{7 + \cos^2 \alpha} = 1$
(C) $\frac{x^2}{1 + \cos^2 \alpha} - \frac{y^2}{7 - \cos^2 \alpha} = 1$ (D) $\frac{x^2}{1 + \cos^2 \alpha} - \frac{y^2}{7 + \cos^2 \alpha} = 1$
(E) $\frac{x^2}{\cos^2 \alpha} - \frac{y^2}{5 - \cos^2 \alpha} = 1$

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- 33. If $\vec{a} = \hat{i} + 2\hat{j} + 2\hat{k}$, $|\vec{b}| = 5$ and the angle between \vec{a} and \vec{b} is $\frac{\pi}{6}$, then the area of the triangle formed by these two vectors as two sides is (D) $\frac{15\sqrt{3}}{2}$ (E) $15\sqrt{3}$ (A) $\frac{15}{4}$ (B) $\frac{15}{2}$ (C) 15 34. If $\vec{a} \cdot \vec{b} = 0$ and $\vec{a} + \vec{b}$ makes an angle of 60° with \vec{a} , then (A) $\left| \vec{a} \right| = 2 \left| \vec{b} \right|$ (B) $2|\vec{a}| = |\vec{b}|$ (C) $\left| \vec{a} \right| = \sqrt{3} \left| \vec{b} \right|$ (D) $\left| \vec{a} \right| = \left| \vec{b} \right|$ (E) $\sqrt{3}|\vec{a}| = |\vec{b}|$ 35. If $\hat{i} + \hat{j}$, $\hat{j} + \hat{k}$, $\hat{i} + \hat{k}$ are the position vectors of the vertices of a triangle ABC taken in order, then ∠A is equal to (A) $\frac{\pi}{2}$ (B) $\frac{\pi}{5}$ (C) $\frac{\pi}{6}$ (D) $\frac{\pi}{4}$ (E) $\frac{\pi}{3}$ 36. Let $\vec{a} = \hat{i} - 2\hat{j} + 3\hat{k}$. If \vec{b} is a vector such that $\vec{a} \cdot \vec{b} = |\vec{b}|^2$ and $|\vec{a} - \vec{b}| = \sqrt{7}$, then $|\vec{b}| = \sqrt{7}$. (A)√7 (B)√3 (C) 7 (E) 7√3 (D) 3 37. If \vec{a}, \vec{b} and \vec{c} are three non-zero vectors such that each one of them being perpendicular to the sum of the other two vectors, then the value of $\left| \vec{a} + \vec{b} + \vec{c} \right|^2$ is
 - (A) $|\vec{a}|^2 + |\vec{b}|^2 + |\vec{c}|^2$ (B) $|\vec{a}| + |\vec{b}| + |\vec{c}|$ (C) $2(|\vec{a}|^2 + |\vec{b}|^2 + |\vec{c}|^2)$ (D) $\frac{1}{2}(|\vec{a}|^2 + |\vec{b}|^2 + |\vec{c}|^2)$ (E) 0

38. Let \vec{u}, \vec{v} and \vec{w} be vectors such that $\vec{u} + \vec{v} + \vec{w} = \vec{0}$. If $|\vec{u}| = 3, |\vec{v}| = 4$ and $|\vec{w}| = 5$ then $\vec{u} \cdot \vec{v} + \vec{v} \cdot \vec{w} + \vec{w} \cdot \vec{u} =$

(A) 0 (B) -25 (C) 25 (D) 50 (E) 47

39. If $\lambda (3\hat{i} + 2\hat{j} - 6\hat{k})$ is a unit vector, then the values of λ are

(A)
$$\pm \frac{1}{7}$$
 (B) ± 7 (C) $\pm \sqrt{43}$
(D) $\pm \frac{1}{\sqrt{43}}$ (E) $\pm \frac{1}{\sqrt{7}}$

40. If the direction cosines of a vector of magnitude 3 are $\frac{2}{3}, \frac{-a}{3}, \frac{2}{3}, a > 0$, then the vector is

- (A) $2\hat{i} + \hat{j} + 2\hat{k}$ (B) $2\hat{i} \hat{j} + 2\hat{k}$ (C) $\hat{i} 2\hat{j} + 2\hat{k}$ (D) $\hat{i} + 2\hat{j} + 2\hat{k}$ (E) $\hat{i} + 2\hat{j} - 2\hat{k}$
- 41. Equation of the plane through the mid-point of the line segment joining the points P(4,5,-10) and Q(-1,2,1) and perpendicular to PQ is
 - (A) $\vec{r} \cdot \left(\frac{3}{2}\hat{i} + \frac{7}{2}\hat{j} \frac{9}{2}\hat{k}\right) = 45$ (B) $\vec{r} \cdot \left(-\hat{i} + 2\hat{j} + \hat{k}\right) = \frac{135}{2}$ (C) $\vec{r} \cdot \left(5\hat{i} + 3\hat{j} 11\hat{k}\right) + \frac{135}{2} = 0$ (D) $\vec{r} \cdot \left(4\hat{i} + 5\hat{j} - 10\hat{k}\right) = 85$ (E) $\vec{r} \cdot \left(5\hat{i} + 3\hat{j} - 11\hat{k}\right) = \frac{135}{2}$

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- 42. The angle between the straight lines $x-1=\frac{2y+3}{3}=\frac{z+5}{2}$ and x=3r+2; y=-2r-1; z=2, where r is a parameter, is
 - (A) $\frac{\pi}{4}$ (B) $\cos^{-1}\left(\frac{-3}{\sqrt{182}}\right)$ (C) $\sin^{-1}\left(\frac{-3}{\sqrt{182}}\right)$ (D) $\frac{\pi}{2}$ (E) 0
- 43. Equation of the line through the point (2,3,1) and parallel to the line of intersection of the planes x-2y-z+5=0 and x+y+3z=6 is

(A)
$$\frac{x-2}{-5} = \frac{y-3}{-4} = \frac{z-1}{3}$$
 (B) $\frac{x-2}{5} = \frac{y-3}{-4} = \frac{z-1}{3}$ (C) $\frac{x-2}{5} = \frac{y-3}{4} = \frac{z-1}{3}$
(D) $\frac{x-2}{4} = \frac{y-3}{3} = \frac{z-1}{2}$ (E) $\frac{x-2}{-4} = \frac{y-3}{-3} = \frac{z-1}{2}$

44. A unit vector parallel to the straight line $\frac{x-2}{3} = \frac{3+y}{-1} = \frac{z-2}{-4}$ is

(A) $\frac{1}{\sqrt{26}}(3\hat{i}-\hat{j}+4\hat{k})$ (B) $\frac{1}{\sqrt{26}}(\hat{i}+3\hat{j}-\hat{k})$ (C) $\frac{1}{\sqrt{26}}(3\hat{i}-\hat{j}-4\hat{k})$ (D) $\frac{1}{\sqrt{26}}(3\hat{i}+\hat{j}+4\hat{k})$ (E) $\frac{1}{\sqrt{26}}(\hat{i}-3\hat{j}+4\hat{k})$

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45. The angle between a normal to the plane 2x - y + 2z - 1 = 0 and the z-axis is (A) $\cos^{-1}\left(\frac{1}{3}\right)$ (B) $\sin^{-1}\left(\frac{2}{3}\right)$ (C) $\cos^{-1}\left(\frac{2}{3}\right)$ (D) $\sin^{-1}\left(\frac{1}{3}\right)$ (E) $\sin^{-1}\left(\frac{3}{5}\right)$

46. Foot of the perpendicular drawn from the origin to the plane 2x-3y+4z=29 is

- (A) (5, -1, 4)(B) (7, -1, 3)(C) (5, -2, 3)(D) (2, -3, 4)(E) (1, -3, 4)
- 47. The distance between the x-axis and the point (3, 12, 5) is
 - (A) 3 (B) 13 (C) 14 (D) 12 (E) 5

48.	If $\sum_{i=1}^{9} (x_i \cdot$	-5)=9	and $\sum_{i=1}^{9} (x_i - 3)$	$\left(5\right)^2 = 45$, then the star	ndard deviation o	of the 9 items
	$x_1, x_2, \cdots,$	x ₉ is				
	(A) 9	1.5	(B) 4	(C) 3	(D) 2	(E) 1

49. If two dice are thrown simultaneously, then the probability that the sum of the numbers which come up on the dice to be more than 5 is

(A) $\frac{5}{36}$. (B) $\frac{1}{6}$ (C) $\frac{5}{18}$ (D) $\frac{7}{18}$ (E) $\frac{13}{18}$

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50. Let A and B be two events such that $P(A \cup B) = P(A) + P(B) - P(A)P(B)$. If 0 < P(A) < 1 and 0 < P(B) < 1, then $P(A \cup B)' =$ (A) 1 - P(A)(B) 1 - P(A')(C) 1 - P(A)P(B)(D) [1 - P(A)]P(B')(E) 1 51. The standard deviation of 9, 16, 23, 30, 37, 44, 51 is (A) 7 (B) 9 (C) 12 (D) 14 (E) 16 The value of $\lim_{x \to 3} \frac{x^5 - 3^5}{x^8 - 3^8}$ is equal to 52. (A) $\frac{5}{8}$ (B) $\frac{5}{64}$ (C) $\frac{5}{216}$ (D) $\frac{1}{27}$ (E) $\frac{1}{63}$ 53. Let $f(x) = (x^5 - 1)(x^3 + 1)$, $g(x) = (x^2 - 1)(x^2 - x + 1)$ and let h(x) be such that f(x) = g(x)h(x). Then $\lim_{x \to 1} h(x)$ is (A) 0 (B) 1 (C) 3 (D) 4 (E) 5 54. $\lim_{x\to 0} \frac{\log(1+3x^2)}{x(e^{5x}-1)} =$ (A) $\frac{3}{5}$ (B) $\frac{5}{3}$ (C) $\frac{-3}{5}$ (D) $\frac{-5}{3}$ (E) 1

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55.	If $f(x) = \frac{x+2}{3x-1}$, then $f(f(x))$)) is		
	(A) <i>x</i>	(B) <i>-x</i>	(C) $\frac{1}{x}$	(D) $-\frac{1}{x}$	(E) 0
56.	Let $f(x) = \begin{cases} ax \\ a^2 x \end{cases}$	$+3, x \le 2$ x-1, x > 2. T	Then the values of a	for which f is conti	inuous for all x are
	(A) 1 and -2 (D) -1 and -2	2	(B) 1 and 2 (E) 0 and 3	(C) –	1 and 2
57.			mbers. Let $f: R \to R$, $y \in R$. Then $f'(x)$		n that
	(A) $f(x)$	(B) 1	(C) 0	(D) x^2	(E) <i>x</i>
58.	Let $f(x) = \int_{1}^{x} \sin x$	$h^2\left(\frac{t}{2}\right)dt$. The	In the value of $\lim_{x\to 0} \frac{J}{x}$	$\frac{f(\pi+x)-f(\pi)}{x}$ is	equal to
	(A) $\frac{1}{4}$	(B) $\frac{1}{2}$	(C) $\frac{3}{4}$	(D) 1	(E) 0

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59.	If $y = f(x^2 + 2)$ and $f'(3) = 5$, then $\frac{dy}{dx}$ at $x = 1$ is						
	(A) 5	(B) 25	(C) 15	(D) 20	(E) 10		

60. Let
$$f(x) = x^2 + bx + 7$$
. If $f'(5) = 2f'\left(\frac{7}{2}\right)$, then the value of b is
(A) 4 (B) 3 (C) -4 (D) -3 (E) 2

61. If
$$x = \sin t$$
 and $y = \tan t$, then $\frac{dy}{dx} =$

(A)
$$\cos^3 t$$
 (B) $\frac{1}{\cos^3 t}$ (C) $\frac{1}{\cos^2 t}$ (D) $\sin^2 t$ (E) $\frac{1}{\sin^2 t}$

- 62. If $x = a \cos^3 \theta$ and $y = a \sin^3 \theta$, then $1 + \left(\frac{dy}{dx}\right)^2$ is
 - (A) $\tan \theta$ (B) $\tan^2 \theta$ (C) 1 (D) $\sec^2 \theta$ (E) $\sec \theta$
- 63. If $y = \sin^{-1} \left(2x\sqrt{1 x^2} \right)$, $-\frac{1}{\sqrt{2}} \le x \le \frac{1}{\sqrt{2}}$, then $\frac{dy}{dx}$ is equal to (A) $\frac{x}{\sqrt{1 - x^2}}$ (B) $\frac{1}{\sqrt{1 - x^2}}$ (C) $\frac{2}{\sqrt{1 - x^2}}$ (D) $\frac{2x}{\sqrt{1 - x^2}}$ (E) $\frac{-2x}{\sqrt{1 - x^2}}$
- 64. A straight line parallel to the line 2x y + 5 = 0 is also a tangent to the curve $y^2 = 4x + 5$. Then the point of contact is
 - (A) (2, 1)(B) (-1, 1)(C) (1, 3)(D) (3, 4)(E) (-1, 2)

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65. The function $f(x) = 2x^3 - 15x^2 + 36x + 6$ is strictly decreasing in the interval (A) (2,3) (B) (- ∞ ,2) (C) (3,4) (D) (- ∞ ,3) \cup (4, ∞) (E) (- ∞ ,2) \cup (3, ∞)

66. The slope of the tangent to the curve $y^2 e^{xy} = 9e^{-3}x^2$ at (-1, 3) is

- (A) $\frac{-15}{2}$ (B) $\frac{-9}{2}$ (C) 15 (D) $\frac{15}{2}$ (E) $\frac{9}{2}$
- 67. The radius of a cylinder is increasing at the rate of 5 cm/min so that its volume is constant. When its radius is 5 cm and height is 3 cm the rate of decreasing of its height is
 (A) 6 cm/min (B) 3 cm/min (C) 4 cm/min (D) 5 cm/min (E) 2 cm/min
- 68. The function $f(x) = \begin{cases} 2x^2 1 & \text{if } 1 \le x \le 4\\ 151 30x & \text{if } 4 < x \le 5 \end{cases}$ is not suitable to apply Rolle's

theorem since

- (A) f(x) is not continuous on [1,5] (B) $f(1) \neq f(5)$
- (C) f(x) is continuous only at x = 4
- (D) f(x) is not differentiable in (4, 5)
- (E) f(x) is not differentiable at x = 4

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69. The slope of the normal to the curve $y = x^2 - \frac{1}{x^2}$ at (-1, 0) is

(A)
$$\frac{1}{4}$$
 (B) $-\frac{1}{4}$ (C) 4 (D) -4 (E) 0

70. The minimum value of $\sin x + \cos x$ is

(A) $\sqrt{2}$ (B) $-\sqrt{2}$ (C) $\frac{1}{\sqrt{2}}$ (D) $-\frac{1}{\sqrt{2}}$ (E) 1

71.
$$\int \frac{1}{x^2 (x^4 + 1)^{\frac{3}{4}}} dx \text{ is equal to}$$

(A) $-\frac{(1 + x^4)^{\frac{3}{4}}}{x} + C.$ (B) $-\frac{(1 + x^4)^{\frac{1}{4}}}{2x} + C$ (C) $-\frac{(1 + x^4)^{\frac{1}{4}}}{x} + C$
(D) $-\frac{(1 + x^4)^{\frac{1}{4}}}{x^2} + C$ (E) $-\frac{(1 + x^4)^{\frac{1}{2}}}{x} + C$

72.
$$\int \frac{(1+x)e^x}{\sin^2(xe^x)} dx$$
 is equal to
(A) $-\cot(e^x) + C$ (B) $\tan(xe^x) + C$ (C) $\tan(e^x) + C$
(D) $\cot(xe^x) + C$ (E) $-\cot(xe^x) + C$

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- 73. $\int \frac{xe^{x}}{(1+x)^{2}} dx \text{ is equal to}$ (A) $\frac{-e^{x}}{x+1} + C$ (B) $\frac{e^{x}}{x+1} + C$ (C) $\frac{xe^{x}}{x+1} + C$ (D) $\frac{-xe^{x}}{x+1} + C$ (E) $\frac{e^{x}}{(x+1)^{2}} + C$ 74. $\int e^{x} (\sin x + 2\cos x) \sin x \, dx \text{ is equal to}$ (A) $e^{x} \cos x + C$ (B) $e^{x} \sin x + C$ (C) $e^{x} \sin^{2} x + C$ (D) $e^{x} \sin 2x + C$ (E) $e^{x} (\cos x + \sin x) + C$ 75. $\int \sqrt{1 + \cos x} \, dx \text{ is equal to}$
 - (A) $2\sin\left(\frac{x}{2}\right) + C$ (B) $\sqrt{2}\sin\left(\frac{x}{2}\right) + C$ (C) $\frac{1}{2}\sin\left(\frac{x}{2}\right) + C$ (D) $\frac{\sqrt{2}}{2}\sin\left(\frac{x}{2}\right) + C$ (E) $2\sqrt{2}\sin\left(\frac{x}{2}\right) + C$



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79. Area bounded by the curves $y = e^x$, $y = e^{-x}$ and the straight line x = 1 is (in sq. units)

(A)
$$e + \frac{1}{e}$$
 (B) $e + \frac{1}{e} + 2$ (C) $e + \frac{1}{e} - 2$ (D) $e - \frac{1}{e} + 2$ (E) $e - \frac{1}{e}$

80. The value of the integral $\int_{1}^{e} \frac{1 + \log x}{3x} dx$ is equal to

(A)
$$\frac{1}{4}$$
 (B) $\frac{1}{2}$ (C) $\frac{3}{4}$ (D) e (E) $\frac{1}{e}$

81. The value of the integral $\int_{0}^{1} \frac{x^3}{1+x^8} dx$ is equal to

(A)
$$\frac{\pi}{8}$$
 (B) $\frac{\pi}{4}$ (C) $\frac{\pi}{16}$ (D) $\frac{\pi}{6}$ (E) $\frac{\pi}{12}$

32. The value of the integral
$$\int_{2}^{4} \left(\frac{\log t}{t}\right) dt$$
 is equal to
(A) $\frac{1}{2}(\log 2)^{2}$ (B) $\frac{5}{2}(\log 2)^{2}$ (C) $\frac{3}{2}(\log 2)^{2}$ (D) $(\log 2)^{2}$ (E) $\frac{3}{2}(\log 2)$

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83. The solution of the differential equation $(kx - y^2)dy = (x^2 - ky)dx$ is

(A) $x^3 - y^3 = 3kxy + C$ (B) $x^3 + y^3 = 3kxy + C$ (C) $x^2 - y^2 = 2kxy + C$ (D) $x^2 + y^2 = 2kxy + C$ (E) $x^3 - y^2 = 3kxy + C$

84. The solution of the differential equation $\frac{dy}{dx} = e^x + 1$ is (A) $y = e^x + C$ (B) $y = x + e^x + C$ (C) $y = xe^x + C$ (D) $y = x(e^x + 1) + C$ (E) $y = e^x + Cx$

85. The order and degree of the differential equation $\frac{d^2 y}{dx^2} + \left(\frac{dy}{dx}\right)^{\frac{3}{2}} = y$ are respectively

(A) 1, 1 (B) 1, 2 (C) 1, 3 (D) 2, 1 (E) 2, 2

86. An integrating factor of the differential equation $\sin x \frac{dy}{dx} + 2y \cos x = 1$ is

(A) $\sin^2 x$ (B) $\frac{2}{\sin x}$ (C) $\log |\sin x|$ (D) $\frac{1}{\sin^2 x}$ (E) $2\sin x$

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87.	If the operation	\oplus is defined b	$y \ a \oplus b = a^2 + b^2$	for all real num	obers a and b , then	
	$(2 \oplus 3) \oplus 4 =$					
	(A) 120	(B) 185	(C) 175	(D) 129	(E) 312	
88.	represents 10%	of the enrolment		nd 12% of the enr	chemistry is 30. This olment in chemistry.	
	(A) 520	(B) 490	(C) 560	(D) 480	(E) 540	
89.	Let $f(x) = x-2 $, where x is a real	l number. Which	one of the followir	ng is true?	
	(A) f is periodic		(B) $f(x+y)$	= f(x) + f(y)		
	(C) f is an odd f	unction	(D) f is not a	a 1-1 function		
	(E) f is an even	function				
90.	If $A = \{1, 3, 5, 7\}$ A into B is	and $B = \{1, 2, 3, 4\}$,5,6,7,8}, then the	e number of one-to	o-one functions from	
	(A) 1340	(B) 1860	(C) 1430	(D) 1880	(E) 1680	

91. The range of the function $f(x) = x^2 + 2x + 2$ is

(A)
$$(1,\infty)$$
 (B) $(2,\infty)$ (C) $(0,\infty)$ (D) $(1,\infty)$ (E) $(-\infty,\infty)$

92. If $f(x) = \sqrt{x}$ and g(x) = 2x - 3, then $(f \circ g)(x)$ is

(A)
$$(-\infty, -3)$$
 (B) $\left(-\infty, -\frac{3}{2}\right)$ (C) $\left[-\frac{3}{2}, 0\right]$
(D) $\left[0, \frac{3}{2}\right]$ (E) $\left[\frac{3}{2}, \infty\right)$

93. If $z = \frac{(\sqrt{3}+i)^3 (3i+4)^2}{(8+6i)^2}$, then |z| is equal to (A) 8 (B) 2 (C) 5 (D) 4

94. Let $w \neq \pm 1$ be a complex number. If |w| = 1 and $z = \frac{w-1}{w+1}$, then $\operatorname{Re}(z)$ is equal to

(A) 1 (B) $\frac{1}{|w+1|}$ (C) Re(w) (D) 0 (E) $w+\overline{w}$

95. If
$$z = e^{2\pi i/3}$$
, then $1 + z + 3z^2 + 2z^3 + 2z^4 + 3z^5$ is equal to
(A) $-3e^{\pi i/3}$ (B) $3e^{\pi i/3}$ (C) $3e^{2\pi i/3}$ (D) $-3e^{2\pi i/3}$ (E) 0

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(E) 10

96.	If $z_1 = 2\sqrt{2}(1+i)$) and $z_2 = 1 + i\sqrt{3}$, then $z_1^2 z_2^3$ is a	equal to	
	(A) 128 i	(B) 64 i	(C) –64 i	(D) -128 <i>i</i>	(E) 256
97.		timbers z_1, z_2 and $z_2^2 + (z_1 - z_3)^2$ is equal to $(z_1 - z_3)^2 = (z_1 - z_3)^2 = (z_1 - z_3)^2$		es of an isosceles tri	iangle, right angled
	(A) 0	(B) $(z_2 + z_3)^2$	(C) 2	(D) 3	(E) $(z_2 - z_3)^2$
98.	If the roots of x^2	-ax+b=0 are two	vo consecutive odd	integers, then a^2 –	-4 <i>b</i> is
				(D) 6	(E) 7
99.	If α and β are the function of β and β are the function of β are the function of β are the function of β and β are the function of β are the function of β and β are the function of β are the functi	he roots of $x^2 - ax$	$+b^2=0$, then α^2	$+\beta^2$ is equal to	
				(D) $a^2 + 2b$	(E) $a^2 - b^2$
100	. If α and β are t	he roots of the equ	ation $x^2 + 3x - 4 =$	0, then $\frac{1}{\alpha} + \frac{1}{\beta}$ is	equal to
	(A) $\frac{-3}{4}$	(B) $\frac{3}{4}$	(C) $\frac{-4}{3}$	(D) $\frac{4}{3}$	(E) $\frac{3}{2}$
				1	

101. The value of x such that $3^{2x} - 2(3^{x+2}) + 81 = 0$ is

(A) 1 (B) 2 (C) 3 (D) 4 (E) 5

102. If the roots of the equation $x^2 + 2bx + c = 0$ are α and β , then $b^2 - c = 0$

(A)
$$\frac{(\alpha - \beta)^2}{4}$$
 (B) $(\alpha + \beta)^2 - \alpha\beta$ (C) $(\alpha + \beta)^2 + \alpha\beta$
(D) $\frac{(\alpha - \beta)^2}{2} + \alpha\beta$ (E) $\frac{(\alpha + \beta)^2}{2} + \alpha\beta$

103. The equation whose roots are the squares of the roots of the equation $2x^2 + 3x + 1 = 0$ is

(A) $4x^2 + 5x + 1 = 0$ (B) $4x^2 - x + 1 = 0$ (C) $4x^2 - 5x - 1 = 0$ (D) $4x^2 - 5x + 1 = 0$ (E) $4x^2 + 5x - 1 = 0$

104. The sum of the series $\sum_{n=8}^{17} \frac{1}{(n+2)(n+3)}$ is equal to (A) $\frac{1}{17}$ (B) $\frac{1}{18}$ (C) $\frac{1}{19}$ (D) $\frac{1}{20}$ (E) $\frac{1}{21}$

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105. If two positiv A.M. and G.M.		the ratio $3+2\sqrt{2}$	$: 3-2\sqrt{2}$, then th	e ratio between their
(A) 6:1	(B) 3:2	(C) 2:1	(D) 3:1	(E) 1:6
106. Let $x_1, x_2, \cdots,$	x_n be in an A.P. If	$f x_1 + x_4 + x_9 + x_{11} +$	$x_{20} + x_{22} + x_{27} + x_{30}$	= 272, then
$x_1 + x_2 + x_3 + \cdots$	$\cdots + x_{30}$ is equal to			
(A) 1020	(B) 1200	(C) 716	(D) 2720	(E) 2072
107. If the second a	and fifth terms of a	G.P. are 24 and 3 re	spectively, then the	sum of first six
terms is				
(A) 181	(B) $\frac{181}{2}$	(C) 189	(D) $\frac{189}{2}$	(E) 191
108. If the sum of	first 75 terms of a	n A.P. is 2625, ther	n the 38 th term of th	ne A.P. is
(A) 39	(B) 37	(C) 36	(D) 38	(E) 35

109. If -5, k, -1 are in A.P., then the value of k is equal to

(A) -5 (B) -3 (C) -1 (D) 3 (E) 5

- 110. Let T_n denote the number of triangles which can be formed by using the vertices of a regular polygon of n sides. If $T_{n+1} T_n = 36$, then n is equal to
 - (A) 2 (B) 5 (C) 6 (D) 8 (E) 9

111. The middle term in the expansion of $\left(\frac{10}{x} + \frac{x}{10}\right)^{10}$ is

(A) ${}^{10}C_5$ (B) ${}^{10}C_6$ (C) ${}^{10}C_5\frac{1}{x^{10}}$ (D) ${}^{10}C_5x^{10}$ (E) ${}^{10}C_510^{10}$

112. The coefficient of x^{49} in the product $(x-1)(x-2)(x-3) \cdots (x-50)$ is (A) -2250 (B) -1275 (C) 1275 (D) 2250 (E) -49

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113. The sum of the coefficients in the binomial expansion of $\left(\frac{1}{x}+2x\right)^6$ is equal to

(A) 1024 (B) 729 (C) 243 (D) 512 (E) 64

114. The value of ${}^{2}P_{1} + {}^{3}P_{1} + ... + {}^{n}P_{1}$ is equal to

(A)
$$\frac{n^2 - n + 2}{2}$$
 (B) $\frac{n^2 + n + 2}{2}$ (C) $\frac{n^2 + n - 1}{2}$
(D) $\frac{n^2 - n - 1}{2}$ (E) $\frac{n^2 + n - 2}{2}$

115. How many four digit numbers *abcd* exist such that a is odd, b is divisible by 3, c is even and d is prime?

(A) 380 (B) 360 (C) 400 (D) 520 (E) 480

116. If a_1, a_2, a_3, \dots are in A.P., then the value of $\begin{vmatrix} a_1 & a_2 & 1 \\ a_2 & a_3 & 1 \\ a_3 & a_4 & 1 \end{vmatrix}$ is equal to

(A)
$$a_4 - a_1$$
 (B) $\frac{a_1 + a_4}{2}$ (C) 1 (D) $\frac{a_2 + a_3}{2}$ (E) 0

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117. If
$$\begin{vmatrix} 2a & x_1 & y_1 \\ 2b & x_2 & y_2 \\ 2c & x_3 & y_3 \end{vmatrix} = \frac{abc}{2} \neq 0$$
, then the area of the triangle whose vertices are $\left(\frac{x_1}{a}, \frac{y_1}{a}\right), \left(\frac{x_2}{b}, \frac{y_2}{b}\right)$ and $\left(\frac{x_3}{c}, \frac{y_3}{c}\right)$ is
(A) $\frac{1}{4}abc$ (B) $\frac{1}{8}abc$ (C) $\frac{1}{4}$ (D) $\frac{1}{8}$ (E) $\frac{1}{12}$
118. The system of linear equations $3x + y - z = 2$, $x - z = 1$ and $2x + 2y + az = 5$ has unique solution when
(A) $a \neq 3$ (B) $a \neq 4$ (C) $a \neq 5$ (D) $a \neq 2$ (E) $a \neq 1$
119. If $A = \begin{bmatrix} 2-k & 2\\ 1 & 3-k \end{bmatrix}$ is a singular matrix, then the value of $5k - k^2$ is equal to
(A) 0 (B) 6 (C) -6 (D) -4 (E) 4
120. If a,b,c are non-zero and different from 1, then the value of $\log_a 1 - \log_a b - \log_a c - \log_a 1 - \log_a (\frac{1}{c}) - \log_a (1 - \frac{1}{c}) -$

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